

## Geometry and Mensuration-Exercise Questions updated on Dec 2024

1. If each side of a square is increased by 50%, the ratio of the area of the resulting square to the area of the given square is:  
a. 5:4    b. 9:4    c. 4:5    d. 4:9
2. A man walking at the speed of 4 kmph crosses a square field diagonally in 3 minutes. The area of the field is:  
a. 18000m<sup>2</sup>    b. 20000m<sup>2</sup>    c. 19000m<sup>2</sup>    d. 25000m<sup>2</sup>
3. The cost of cultivating a square field at the rate of Rs.135 per hectare is Rs.1215. The cost of putting a fence around it at the rate of 75 paise per meter would be :  
a. Rs.360    b. Rs.810    c. Rs.900    d. Rs.1800
4. The cost of carpeting a room 18m long with a carpet 75cm wide at 45 paise per meter is Rs.81. The breadth of the room is:  
a. 7m    b. 7.5m    c. 8m    d. 8.5m
5. A hall 36m long and 15m broad is to be paved with stones, each measuring 6dm by 5 dm. The number of stones required is:  
a. 180    b. 1800    c. 18    d. 18000
6. A room 5.44m long and 3.74m broad is to be paved with square tiles. The least number of square tiles required to cover the floor is:  
a. 176    b. 192    c. 184    d. 162
7. A man cycles round the boundary of a rectangular park at the rate of 12 kmph and completes one full round in 8 minutes. If the ratio between the length and breadth of the park be 3:2, then its area is:  
a. 1536m<sup>2</sup>    b. 15360m<sup>2</sup>    c. 153600m<sup>2</sup>    d. None of these
8. A rectangular carpet has an area of 60 sq.m. If its diagonal and longer side together equal 5 times the shorter side, the length of the carpet is:  
a. 5m    b. 12m    c. 13m    d. 14.5m

9. The cost of papering the four walls of a room is Rs.475. Each one of the length, breadth and height of another room is double that of this room. The cost of papering the walls of this new room is:
- a. Rs.950      b. Rs.1425      c. Rs.1900      d. Rs.712.50
10. The height of a room to its semi-perimeter is 2:5. It costs Rs.260 to paper the walls of the room with paper 50cm wide at Rs.2 per meter allowing an area of 15 sq.m for doors and windows. The height of the room is:
- a. 2.6m      b. 3.9m      c. 4m      d. 4.2m
11. The cross section of a canal is trapezium in shape. The canal is 12m wide at the top and 8m wide at the bottom. If the area of the cross section is 840 sq.m, the depth of the canal is:
- a. 42m      b. 84m      c. 63m      d. 8.75m
12. The altitude of an equilateral triangle of side  $3\sqrt{3}$ cm is:
- a. 3cm      b. 23cm      c. 4.5cm      d.  $\frac{3}{4}$  cm
13. The area of a right-angled triangle is 30 sq.cm and the length of its hypotenuse is 13cm. The length of the shorter leg is:
- a. 4cm      b. 5cm      c. 6cm      d. 7cm
14. The difference between the circumference and the radius of a circle is 37 cm. The area of the circle is:
- a.  $111 \text{ cm}^2$       b.  $148 \text{ cm}^2$       c.  $154 \text{ cm}^2$       d.  $259 \text{ cm}^2$
15. A circular road runs round a circular ground. If the difference between the circumferences of the outer circle and inner circle is 66 metres, the width of the road is:
- a. 5.25m      b. 7m      c. 10.5m      d. 21m
16. A toothed wheel of diameter 50cm is attached to a smaller wheel of diameter 30cm. How many revolutions will the smaller wheel make when the larger one makes 15 revolutions?
- a. 18      b. 20      c. 25      d. 30

17. A circular wire of radius 42cm is cut and bent into the form of a rectangle whose sides are in the ratio of 6:5. The smaller side of the rectangle is:
- a. 30cm      b. 60cm      c. 72cm      d. 132cm.
18. Four horses are tethered at four corners of a square plot of side 63 metres so that they just cannot reach one another. The area left ungrazed is:
- a.  $675.5\text{m}^2$       b.  $780.6\text{m}^2$       c.  $785.8\text{m}^2$       d.  $850.5\text{m}^2$
19. A theater is of the shape as shown below. The cross section is a rectangle  $8\text{m} \times 4\text{m}$  mounted by a triangle of altitude 3m. If the length of the building is 25m, find its volume (Inner measures are given).
- a.  $1100\text{cm}^3$       b.  $1110\text{cm}^3$       c.  $1010\text{cm}^3$       d. None of these
20. The measurement of a rectangular box with lid is  $25\text{cm} \times 12\text{cm} \times 18\text{cm}$ . Find the volume of the largest sphere that can be inscribed in the box (in terms of  $\pi\text{cm}^3$ ). (Hint: The lowest measure of rectangular box represents the diameter of the largest sphere)
- a. 288      b. 48      c. 72      d. 864

**Answer & Explanations:**

1. Ans:b

Let, each side= $a$ . Then, original area= $a^2$ .

New side= $150a/100=3a/2$ . New area= $9a^2/4$ .

Required ratio= $9a^2/4:a^2=9:4$

2. Ans: b.

Length of the diagonal= Distance covered in 3 min. at 4 km/hr.

=  $(4000/60 * 3)=200\text{m}$ .

Therefore, Area of the field=  $1/2 * \text{diagonal}^2$

=  $1/2 * 200*200 = 20000 \text{ m}^2$

3. Ans:c

Area= Total cost/ Rate=  $(1215/135)$  hectares=  $(9*10000)$  sq.m.

Therefore, side of the square=  $\sqrt{90000}=300\text{m}$ .

Perimeter of the field=  $(300*4)\text{m}=1200\text{m}$

Cost of fencing= Rs. $(1200*3/4)=$  Rs.900

4. Ans:b

Length of the carpet= Total cost/ rate/m=  $8100/45=180\text{m}$

Area of the carpet=  $180*75/100=135\text{m}^2$

Breadth of the room =  $(\text{Area}/ \text{length})=135/18=7.5\text{m}$

5. Ans: b

Area of the hall=  $3600*1500$

Area of each stone=  $(60*50)$

Therefore, number of stones=  $(3600*1500/ 60*50)=1800$

6. Ans: a

Area of the room=  $544*374 \text{ sq.cm}$

Size of largest square tile= HCF of 544 cm & 374cm

Area of 1 tile=  $34 \times 34$  sq.cm

Therefore, number of tiles=  $(544 \times 374 / 34 \times 34) = 176$

7. Ans:c

Perimeter= Distance covered in 8 min

=  $(12000/60 \times 8)m = 1600m$

Let, length=  $3x$  meters and breadth=  $2x$  meters

Then,  $2(3x+2x) = 1600$  or  $x = 160$

Therefore, length=  $480$  m and breadth=  $320$ m

Therefore, area=  $(480 \times 320)m^2 = 153600 m^2$

8. Ans: b

Let, length=  $x$  meters and breadth=  $y$  meters

Then  $xy=60$  and  $(x^2+y^2) + x = 5$

Therefore,  $x=60$  and  $(x^2+y^2) = (5y-x)^2$

Or  $xy=60$  and  $24y^2-10xy=0$ .

Therefore,  $24y^2-10 \times 60=0$  or  $y^2 = 25$  or  $y=5$ .

Therefore,  $x = (60/5)m = 12m$ . So, length of the carpet =  $12m$

9. Ans:c

Let the dimensions of former room be  $x, y$  and  $z$ .

Then, the area of its 4 walls=  $2(x+y) \times z$  sq. units.

Dimensions of another room are  $2x, 2y$  and  $2z$  units.

Therefore, area of 4 walls of this room=  $2(2x+2) \times 2z = 4 \times [2(x+y) \times z]$

=  $4$  (Area of 4 walls of 1st room)

Therefore, required cost= Rs.  $(475 \times 4) =$  Rs.1900

10. Ans:c

Let, height=  $2x$  metres & (length+ breadth)=  $5x$  metres.

Length of paper=  $(260/2)m = 130m$ .

Therefore, area of paper=  $(130 \times 50 / 100) = 65\text{m}^2$

Area of 4 walls=  $(65 + 15) = 80\text{m}^2$

$2(\text{length} + \text{breadth}) \times \text{height} = 80$ .

Therefore,  $2 \times 5x \times 2x = 80$  or  $x^2 = 4$  or  $x = 2$

Therefore, height of the room= 4m

11. Ans:b

$\frac{1}{2}(12+8)d = 840$  or  $d = 84\text{m}$

12. Ans:c

Area=  $\frac{3}{4} \times (33)^2 = 273/4$ .

Therefore height=  $273/4 \times 2 / 33 = 9/2 = 4.5\text{cm}$

13. Ans:b

Let the other sides be  $x$  and  $y$ . Then,

$x^2 + y^2 = 13^2 = 169$ . Also,  $\frac{1}{2}xy = 30 \Rightarrow xy = 60$ .

Therefore,  $(x+y) = ((x^2+y^2) + 2xy) = (169+120) = 289 = 17$ .

$(x-y) = ((x^2+y^2) - 2xy) = (169-120) = 49 = 7$ .

Solving  $x+y=17$ ,  $x-y=7$ , we get  $x=12$  and  $y=5$ .

Therefore, shorter side = 5cm

14. Ans: c

$2\pi r - r = 37$  or  $(2\pi - 1)r = 37$ .

Or  $(2 \times 22/7 - 1)r = 37$  or  $37r/7 = 37$  or  $r = 7$ .

Therefore, Area=  $\pi r^2 = (22/7 \times 7 \times 7) = 154\text{ cm}^2$

15. Ans:c

$2\pi(R-r) = 60 \Rightarrow 2 \times 22/7 \times (R-r) = 60$ .

Therefore,  $(R-r) = (66 \times 7 / 44) = 10.5\text{m}$

16. Ans: c

Distance moved by toothed wheel in 15 revolutions=  $(15 \times 2 \times \frac{22}{7} \times 25)$

Distance moved by smaller wheel in 1 revolution=  $(2 \times \frac{22}{7} \times 15)$

Therefore, required number of revolutions=  $(15 \times \frac{44}{7} \times 25 \times \frac{7}{44 \times 15}) = 25$

17. Ans: b

Length of wire= circumference of circle of radius 42cm=  $(2 \times \frac{22}{7} \times 42) = 264$ cm.

Therefore, perimeter of rectangle= 264 cm.

Let, length= 6x cm & breadth= 5x cm.

Therefore,  $2(6x+5x) = 264$  or  $x=12$ .

Therefore, smaller side= 60 cm

18. Ans: d

Required area=  $(63 \times 63 - 4 \times \frac{1}{4} \times \frac{22}{7} \times \frac{63}{2} \times \frac{63}{2}) = 850.5$ m<sup>2</sup>

19. Ans: a

Volume of theater= Volume of lower portion+ volume of upper portion.

Volume of lower portion (Rectangular prism)=  $l \times b \times h = 8 \times 4 \times 25 = 800$ cm<sup>3</sup>

Volume of upper portion (triangular prism)=  $(\frac{1}{2} \times b \times h) \times h = \frac{1}{2} \times 8 \times 3 \times 25 = 300$  cm<sup>3</sup>

Therefore, Total volume= Volume of lower portion+ volume of upper portion  
=  $800+300 = 1100$ cm<sup>3</sup>

20. Ans: a

$d=12$ ,  $r=6$ ;

Volume of the largest sphere=  $\frac{4}{3}\pi r^3$   
=  $\frac{4}{3} \times \pi \times 6 \times 6 \times 6 = 288\pi$ cm<sup>3</sup>